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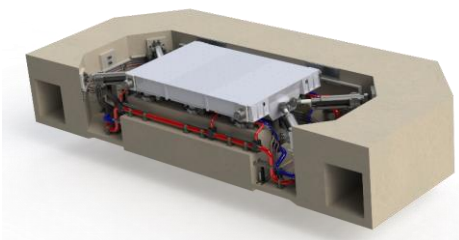
Natural Hazards Engineering Research Infrastructure



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Structural Engineering

Soil-Structure Interaction Issues

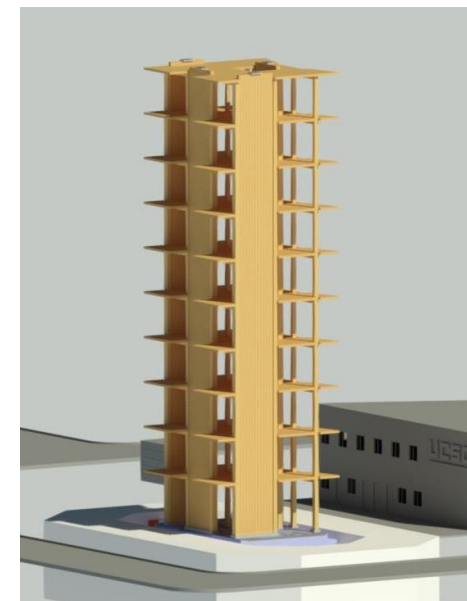
Scott J. Brandenberg, UCLA



NHERI@UC San Diego User Training Workshop



December 15-16, 2022
University of California, San Diego



Motivation

- Soil-structure interaction (SSI) is coupling of structural and soil responses
- SSI can be modeled using techniques ranging from simple (e.g., “springs” attached to the base of structural elements) to complex (e.g., 3D nonlinear effective stress analysis combining soil and structural elements).
- However, it is very often ignored. Why?

Motivation

- SSI requires effective communication between structural and geotechnical engineers.



Outline

- Two recent SSI research projects on topics for which geotechnical engineers generally ignore SSI, but including it is important:
 1. Seismic earth pressures acting on flexible vertical retaining walls
 2. Influence of shallow foundations on earthquake-induced ground failure potential

Collaborators



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Khalifa University

Seismic Earth Pressures

Seismic Earth Pressures

Consider case of vertically propagating, horizontally coherent, SH wave

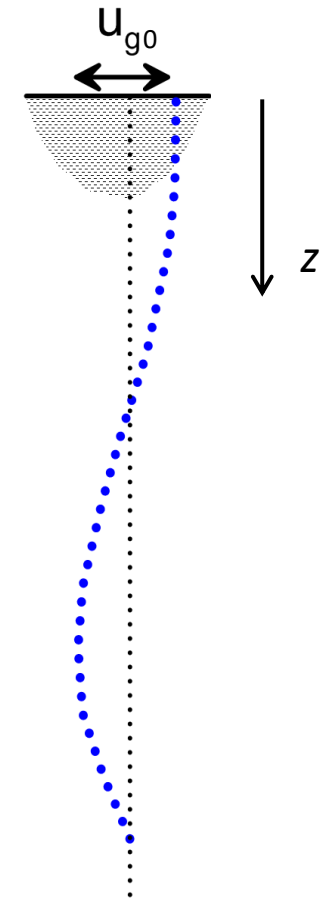
$$\text{Acceleration: } \ddot{u}_g(z) = -\omega^2 u_{g0} \cos\left(\frac{\omega z}{V_s}\right) e^{i\omega t}$$

Inertia generated by wave resisted by mobilized shear stresses, $\tau_{hv}(z)$

Wave produces no change in normal stresses on vertical or horizontal planes (absent soil plasticity)

If we were to make an excavation and replace the excavated soil with a structural system with the exact same mass and stiffness as the excavated soil, seismic earth pressures would be zero

\therefore Horizontal stresses have no fundamental association with acceleration. Rather, it is relative displacement between the soil and wall that creates earth pressure.



Seismic Earth Pressures

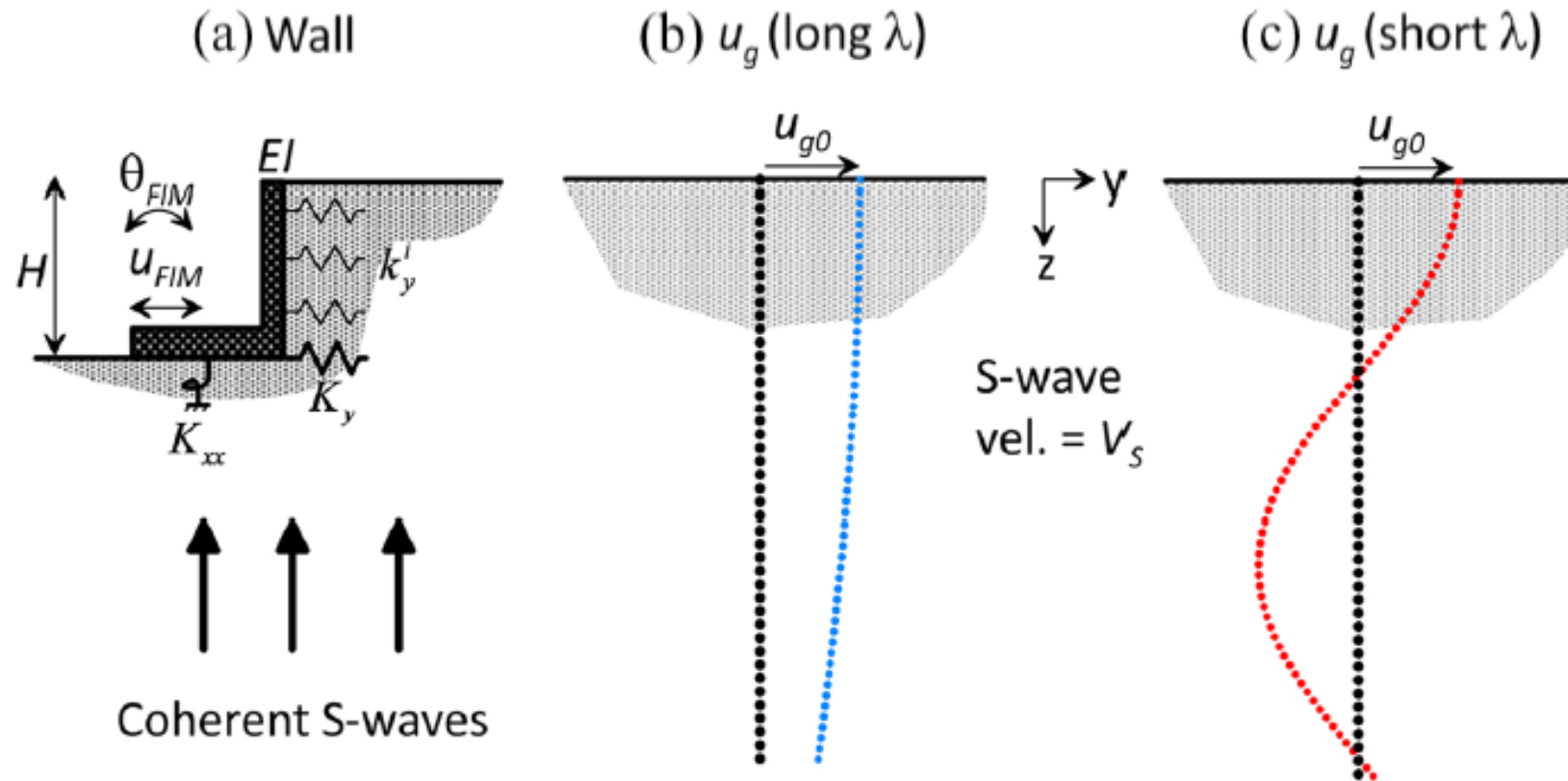


Figure 2. Schematic illustration of free-standing retaining wall subjected to seismic waves with different wavelengths (a) wall, (b) u_g (long λ), and (c) u_g (short λ).

Durante et al. (2022), BSSC (2020).

Seismic Earth Pressures

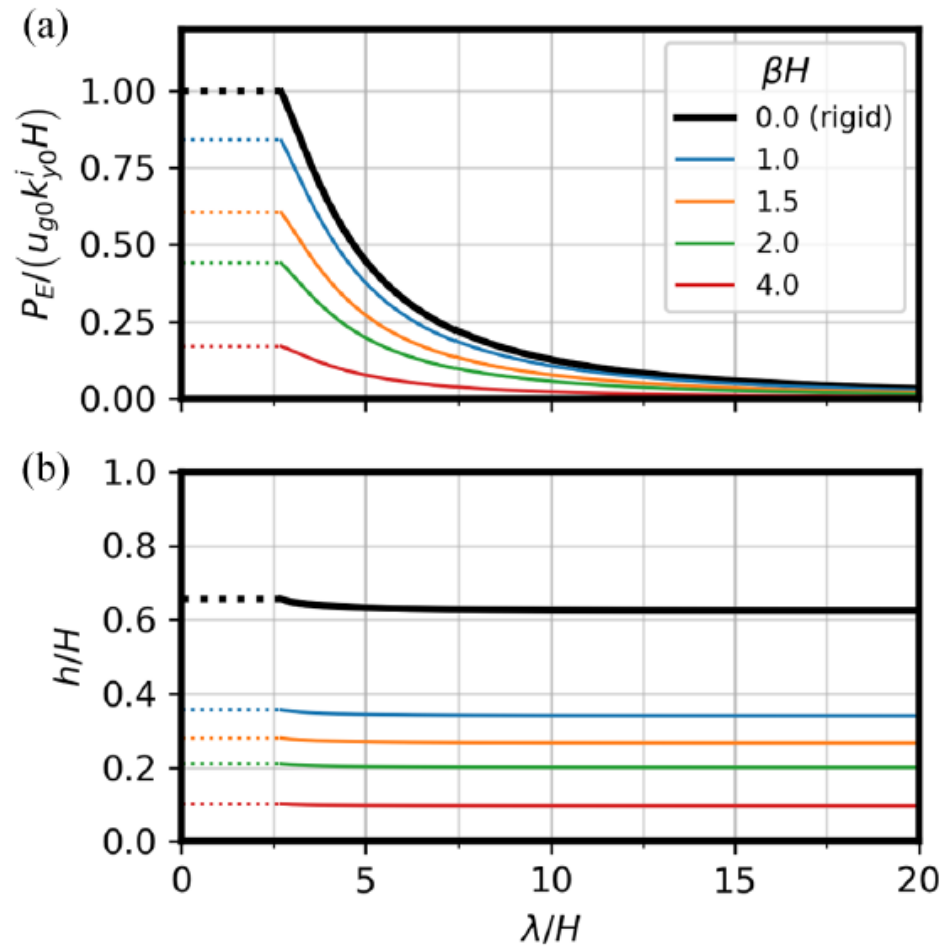


Figure 3. Variation with normalized wavelength λ/H of (a) normalized amplitude of P_E and (b) its point of application above the wall base for various values of βH . Dotted lines at low λ/H are approximations of exact solution.

$$EI \frac{\partial^4 u_w}{\partial z^4} + k_y^i [u_{g0} \cos(kz) - u_w] = 0$$

$$\beta = \sqrt[4]{\frac{k_y^i}{4EI}}$$

$$u_{g0} = f_u P_{GV} / \omega_m$$

$$f_u = \begin{cases} 0.65 & \text{if } \lambda/H < 2.5 \\ 0.95 & \text{if } \lambda/H > 20 \\ 0.607 + 0.017\lambda/H & \text{otherwise} \end{cases}$$

$$\frac{P_E}{P_{E,rigid}} = \xi = \begin{cases} 1 - \exp\left(1 - \frac{2.9}{\beta H}\right) & \beta H < 1 \\ \sin\left(-0.45 + \frac{1.43}{\beta H}\right) + \cos\left(1.22 + \frac{0.34}{\beta H}\right) & \beta H \geq 1 \end{cases}$$

$$\frac{h}{H} = \begin{cases} 0.6 - \exp\left(-0.12 - \frac{2.8}{\beta H}\right) & \beta H < 1 \\ \sin\left(1.68 + \frac{1.5}{\beta H}\right) + \cos\left(2.87 - \frac{1.92}{\beta H}\right) & \beta H \geq 1 \end{cases}$$

Durante et al. (2022), BSSC (2020).

Seismic Earth Pressures

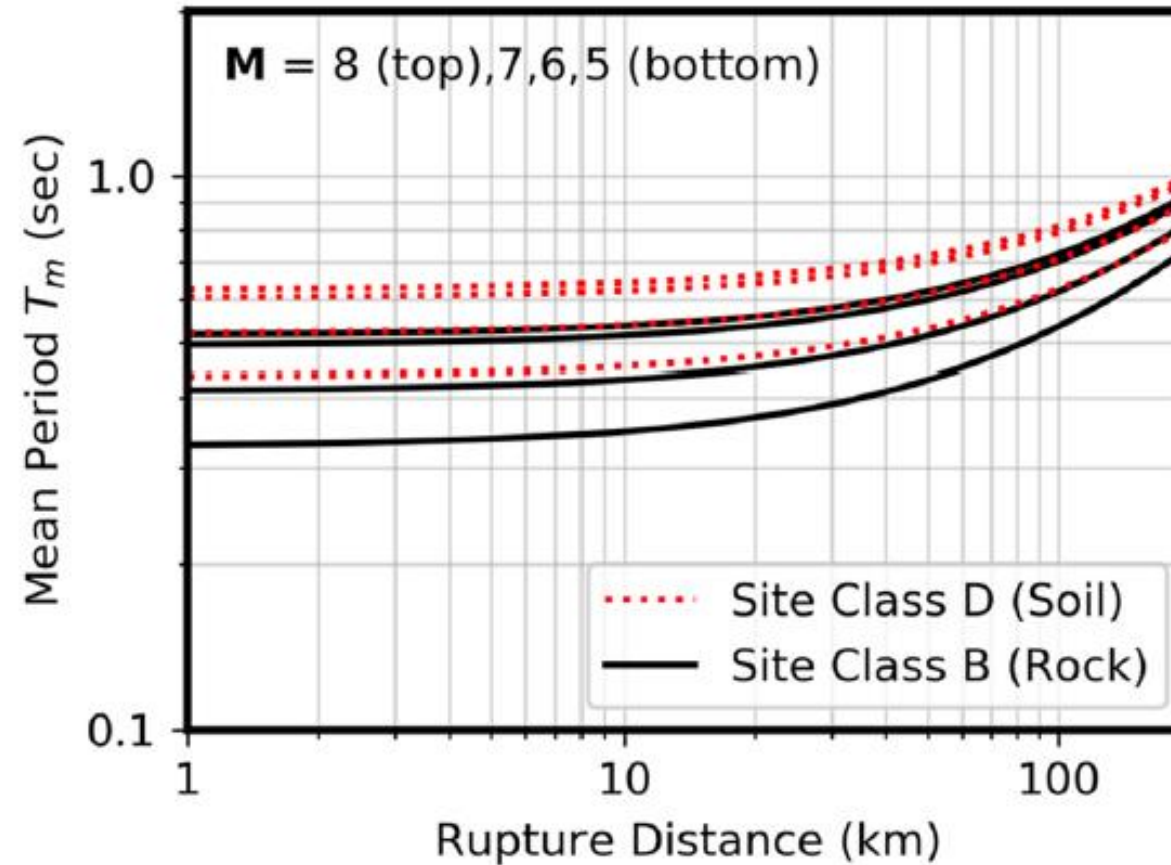


Figure 4. Variation of median values of mean period (T_m) with magnitude, distance, and site condition (Rathje et al., 2004).

Durante et al. (2022), BSSC (2020)

Seismic Earth Pressures

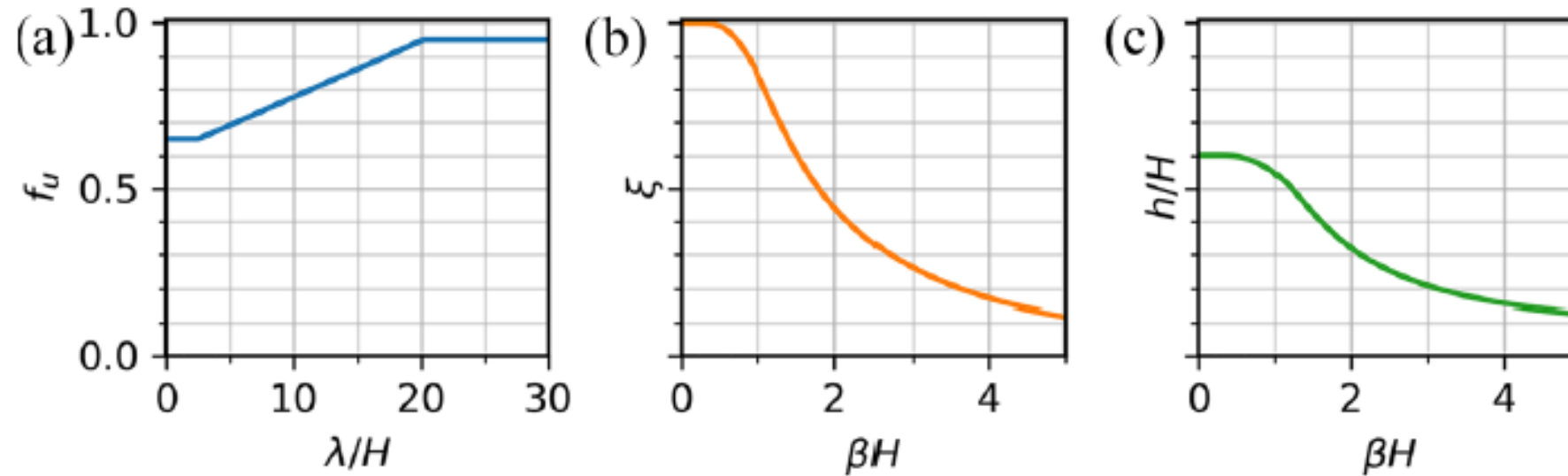


Figure 5. Ground motion amplitude adjustment factor for use with simplified method for evaluation of amplitude of seismic earth pressure resultant force, P_E .

Durante et al. (2022), BSSC (2020)

Seismic Earth Pressures



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NEES-2010-0943: SEISMIC EARTH PRESSURES ON RETAINING STRUCTURES

PIs Nicholas Sitar **Organizations** University of California, Berkeley CA, United States

NEES ID NEES-2010-0943 **Sponsor** [NSF-0936376](#)

Project Type NEES **Start Date** 2009-08-01T00:00:00

DOIs [View All DOIs](#)

Description

Seismic Earth Pressures

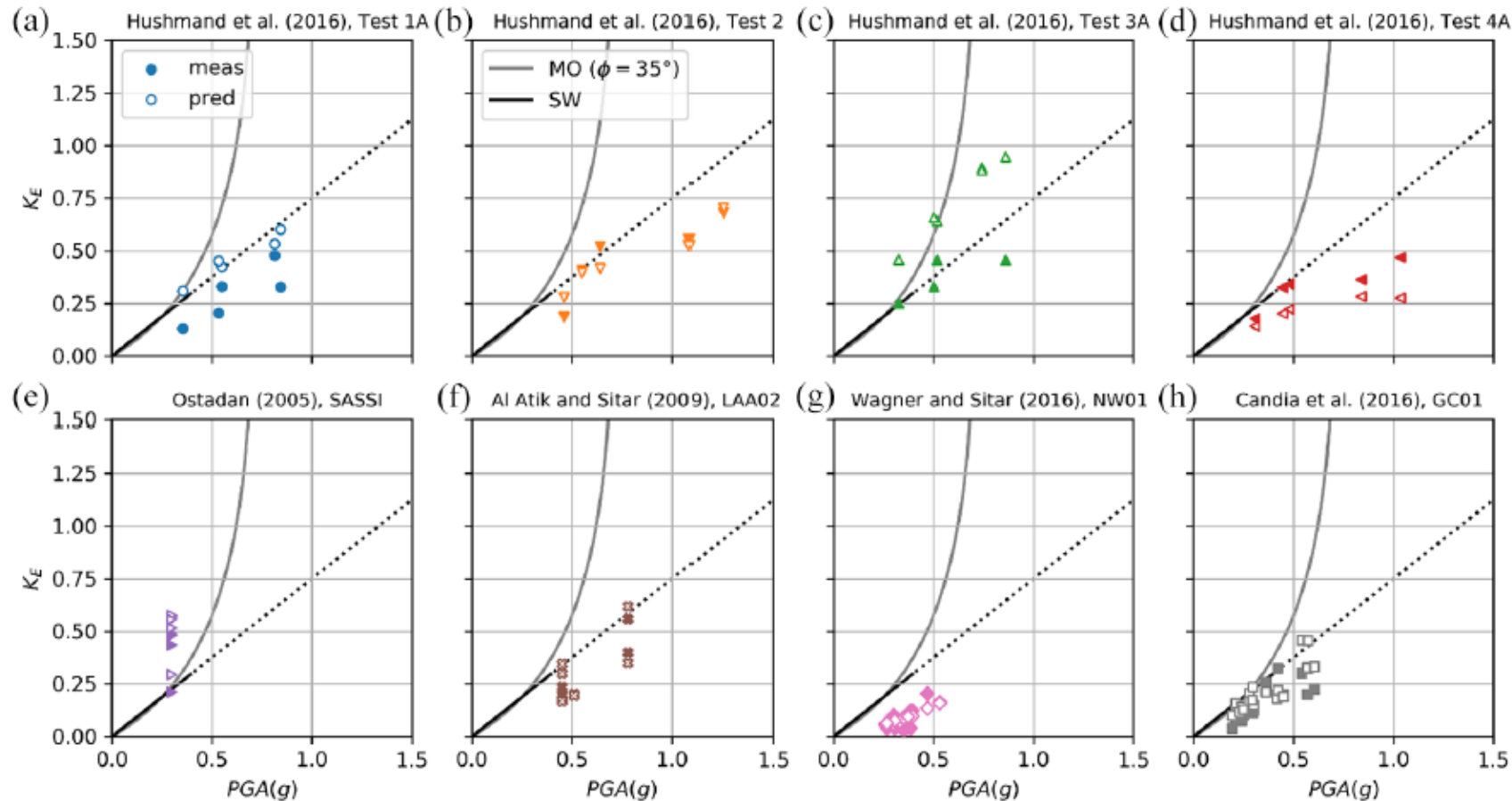


Figure 6. Measured and predicted earth pressure coefficients, K_E , versus PGA . The “predicted” values are from the single-frequency simplified procedure presented in this article. (a) Hushmand et al. (2016), Test 1A; (b) Hushmand et al. (2016), Test 2; (c) Hushmand et al. (2016), Test 3A; (d) Hushmand et al. (2016), Test 4A; (e) Ostadan (2005) SASSI analyses; (f) Al Atik and Sitar (2009), Test LAA02; (g) Wagner and Sitar (2016), test NW01; and (h) Candia et al. (2016), test GC01.

Durante et al. (2022).

Seismic Earth Pressures

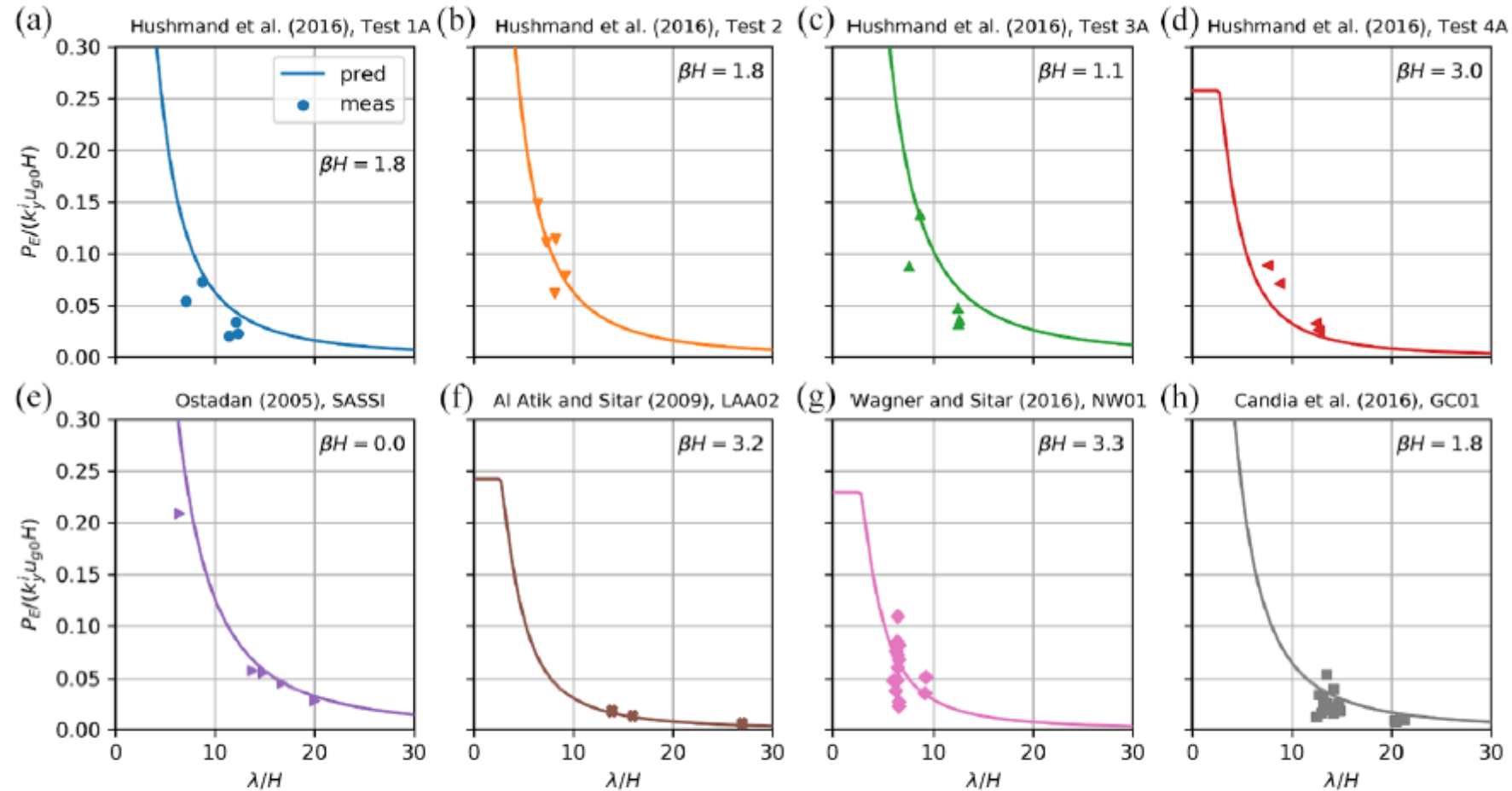


Figure 7. Dimensionless earth pressure, $P_E / (k_y^i u_{g0} H)$, versus wavelength-to-height ratio, λ / H (a) Hushmand et al. (2016), Test 1A; (b) Hushmand et al. (2016), Test 2; (c) Hushmand et al. (2016), Test 3A; (d) Hushmand et al. (2016), Test 4A; (e) Ostadan (2005), SASSI analyses; (f) Al Atik and Sitar (2009), Test LAA02; (g) Wagner and Sitar (2016), Test NW01; and (h) Candia et al. (2016), Test GC01.

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Seismic Earth Pressures

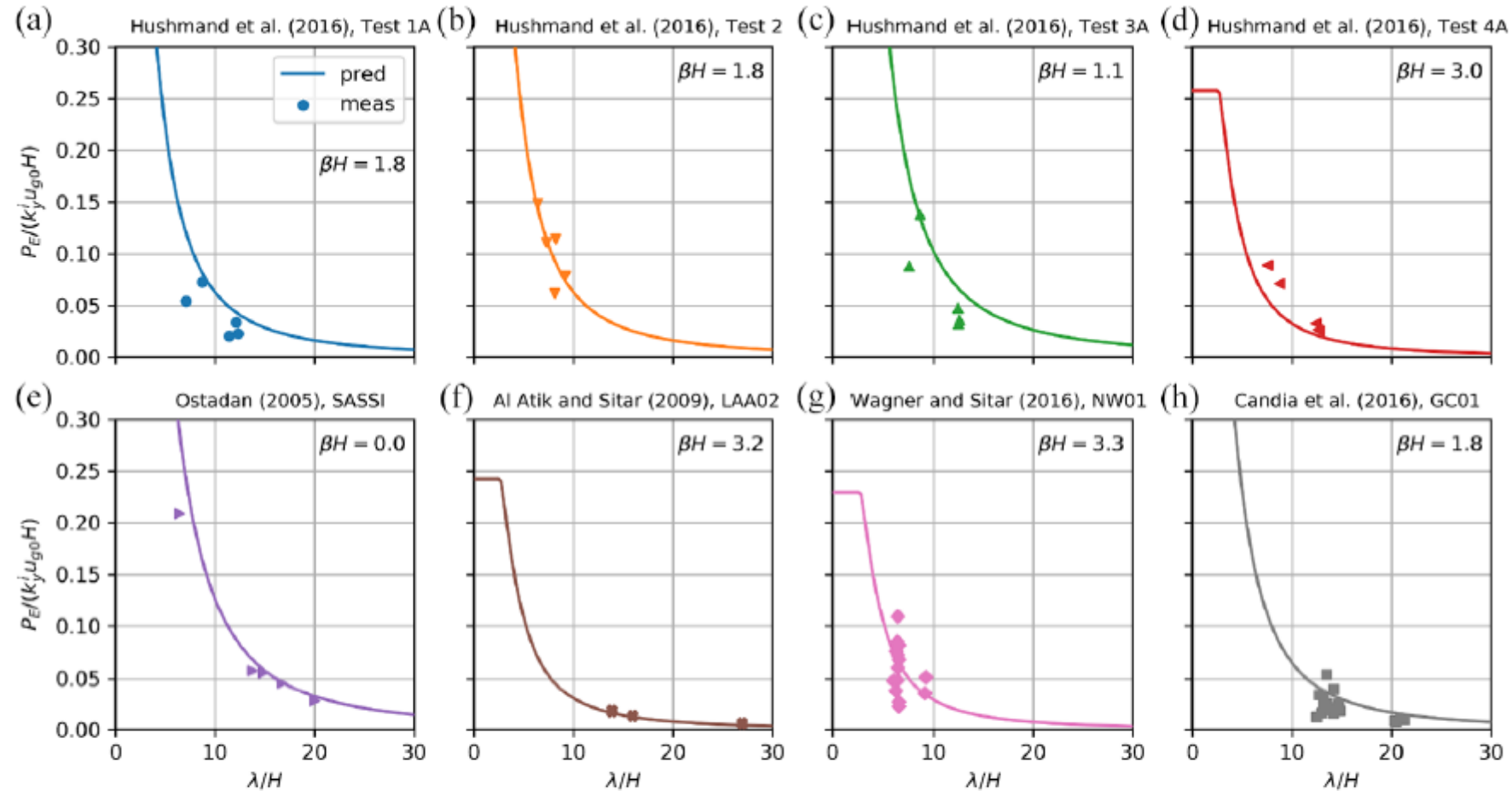


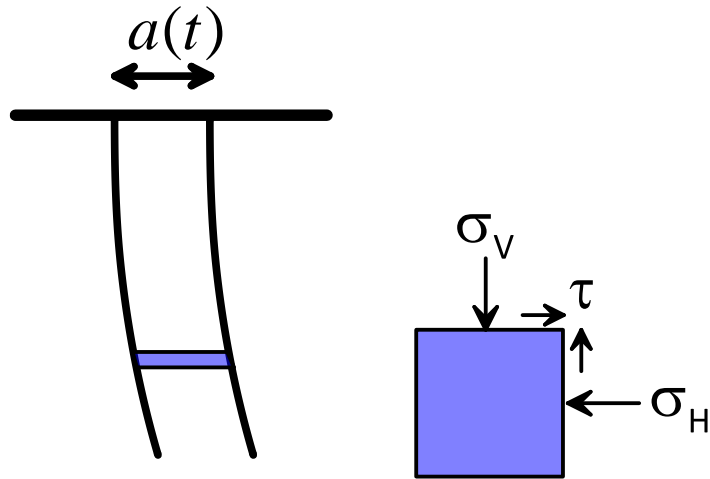
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Durante et al. (2022).

Ground Failure

SSI Effects on Ground Failure

Free-Field Level Ground



Cyclic Stress Ratio

$$CSR = r_e \cdot \frac{a_{\max}}{g} \cdot \frac{\sigma_{vo}}{\sigma'_{vo}} \cdot r_d = 0.65 \cdot \tau_{\max}$$

Cauchy Stress Tensor

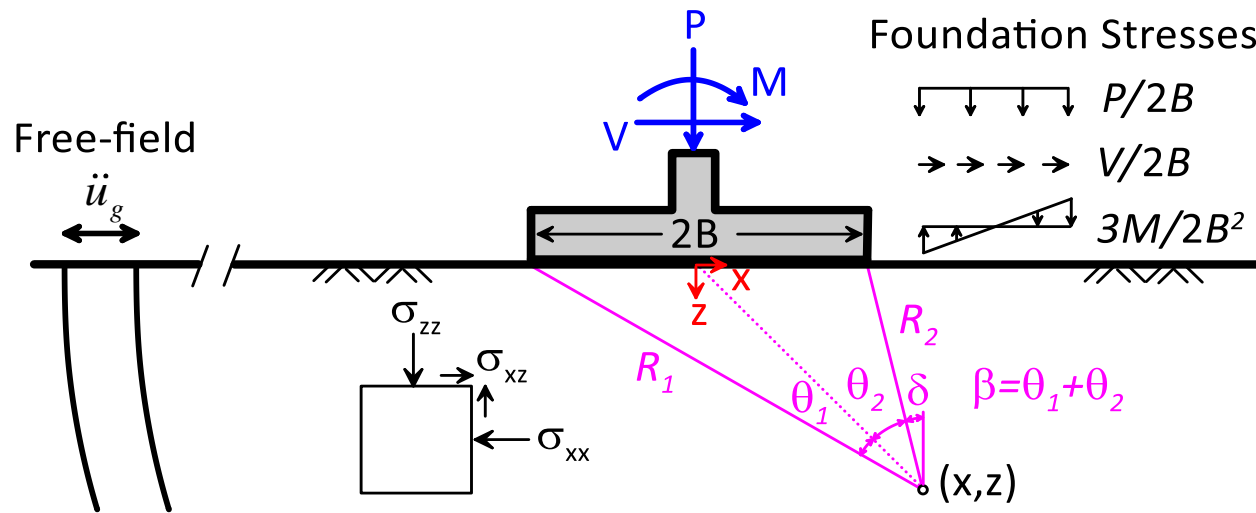
$$\underbrace{\begin{bmatrix} \sigma_v & 0 & 0 \\ 0 & \sigma_H & 0 \\ 0 & 0 & \sigma_H \end{bmatrix}}_{\sigma_o} + \underbrace{\begin{bmatrix} 0 & \tau & 0 \\ \tau & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}}_{\Delta\sigma} = \underbrace{\begin{bmatrix} \sigma_v & \tau & 0 \\ \tau & \sigma_H & 0 \\ 0 & 0 & \sigma_H \end{bmatrix}}_{\sigma}$$



FIGURE 11. View of a 10- to 15-m diameter sand boil deposit about 100 m east of Kornbloom Road (Site 15); this is one of the largest sand boils that erupted during the 1981 event. (Photograph by John Sarmiento.)

SSI Effects on Ground Failure

Brandenberg et al. (2022)



Cauchy Stress Tensor

$$\underbrace{\begin{bmatrix} \sigma_{xx,o} & \sigma_{xy,o} & \sigma_{xz,o} \\ \sigma_{yx,o} & \sigma_{yy,o} & \sigma_{yz,o} \\ \sigma_{zx,o} & \sigma_{zy,o} & \sigma_{zz,o} \end{bmatrix}}_{\sigma_o} + \underbrace{\begin{bmatrix} \Delta\sigma_{xx} & \Delta\sigma_{xy} & \Delta\sigma_{xz} \\ \Delta\sigma_{yx} & \Delta\sigma_{yy} & \Delta\sigma_{yz} \\ \Delta\sigma_{zx} & \Delta\sigma_{zy} & \Delta\sigma_{zz} \end{bmatrix}}_{\Delta\sigma} = \underbrace{\begin{bmatrix} \sigma_{xx} & \sigma_{xy} & \sigma_{xz} \\ \sigma_{yx} & \sigma_{yy} & \sigma_{yz} \\ \sigma_{zx} & \sigma_{zy} & \sigma_{zz} \end{bmatrix}}_{\sigma}$$

Cyclic Stress Ratio

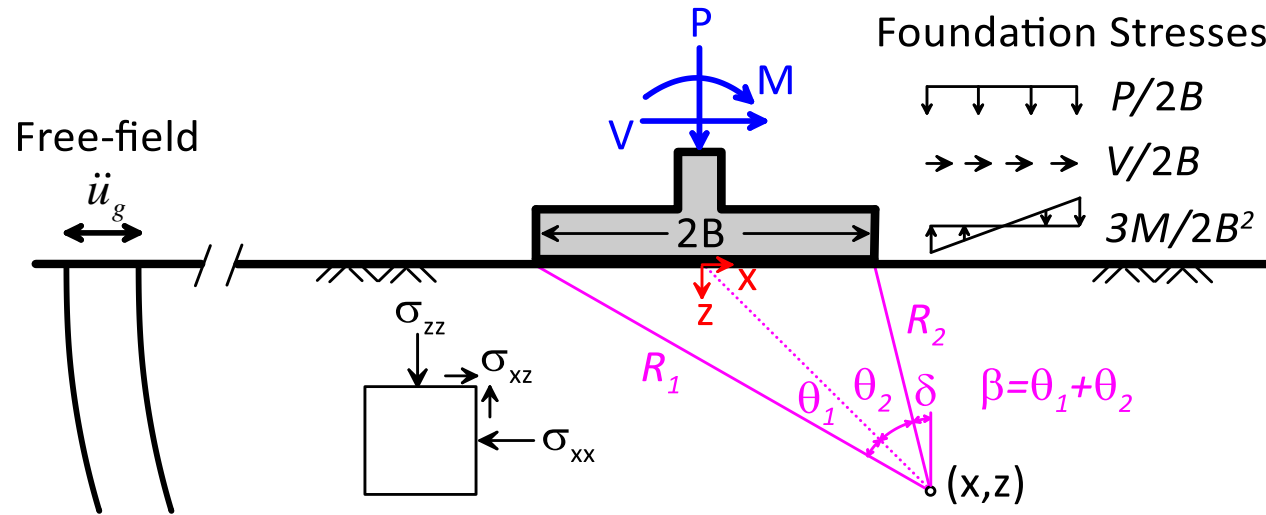
$$CSR = ???$$



Overturning of building B1 as seen from the North-West after the Kocaeli event.
(Photo by Jonathan D. Bray)

PEER (2000). Documenting Incidents of Ground Failure Resulting from the August 17, 1999 Kocaeli, Turkey Earthquake.
<https://apps.peer.berkeley.edu/publications/turkey/adapazari/index.html>

SSI Effects on Ground Failure



Free-field Stresses

$$\begin{aligned}\sigma_{z z o, f f} &= \rho g z \\ \sigma_{x x o, f f} &= \sigma_{y y o, f f} = (\rho g z - u) K_o + u \\ \Delta \sigma_{x z, f f} &= \ddot{u}_g \rho z r_d\end{aligned}$$

Assumptions

1. Flexible strip footing
2. Soil is isotropic elastic halfspace
3. Loading frequency is low enough that static solutions are reasonably accurate

SSI Stresses

$$\begin{aligned}\sigma_{z z, s s i} &= \frac{P}{2 B \pi} [\beta + \sin \beta \cos (\beta + 2 \delta)] + \frac{V}{2 B \pi} [\sin \beta \sin (\beta + 2 \delta)] \\ &\quad + \frac{3 M}{4 B^2 \pi} \left[\frac{2 x}{B} \beta - \sin 2 \delta - \sin (2 \beta + 2 \delta) \right] \\ \sigma_{x x, s s i} &= \frac{P}{2 B \pi} [\beta - \sin \beta \cos (\beta + 2 \delta)] + \frac{V}{2 B \pi} \left[\ln \left(R_1^2 / R_2^2 \right) - \sin \beta \sin (\beta + 2 \delta) \right] \\ &\quad + \frac{3 M}{4 B^2 \pi} \left[\frac{2 x}{B} \beta + \frac{2 z}{B} \left(\ln \left[R_2^2 \right] - \ln \left[R_1^2 \right] \right) + \sin 2 \delta + \sin (2 \beta + 2 \delta) \right] \\ \sigma_{x z, s s i} &= \frac{P}{2 B \pi} [\sin \beta \sin (\beta + 2 \delta)] + \frac{V}{2 B \pi} [\beta - \sin \beta \cos (\beta + 2 \delta)] \\ &\quad + \frac{3 M}{4 B^2 \pi} \left[\cos 2 \delta - \cos (2 \beta + 2 \delta) + \frac{2 z}{B} (\theta_1 - \theta_2) \right]\end{aligned}$$

SSI Effects on Ground Failure

$$\begin{Bmatrix} \sigma_1 \\ \sigma_2 \\ \sigma_3 \end{Bmatrix} = \text{eigenvals} \left(\begin{bmatrix} \sigma_{xx} & \sigma_{xy} & \sigma_{xz} \\ \sigma_{yx} & \sigma_{yy} & \sigma_{yz} \\ \sigma_{zx} & \sigma_{zy} & \sigma_{zz} \end{bmatrix} \right)$$

Principal stresses

$$q = \sqrt{\frac{1}{2} [(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_1 - \sigma_3)^2]}$$

Deviatoric stress invariant

$$p_o' = \frac{\sigma_1' + \sigma_2' + \sigma_3'}{3} = \frac{1}{3} \text{tr}(\sigma')$$

Mean effective stress

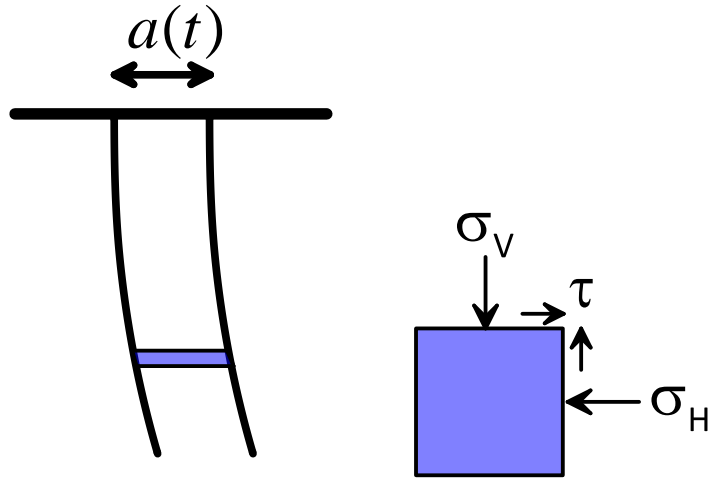
$$CSR = r_e \frac{\sigma_{vo}}{\sigma_{vo}'} \frac{a_{max}}{g} r_d = r_e \frac{\tau}{\sigma_{vo}'}$$

Classical definition of cyclic stress ratio

Brandenberg et al. (2022)

SSI Effects on Ground Failure

Free-Field Level Ground



$$CSR = r_e \frac{\sigma_{vo}}{\sigma_{vo}'} \frac{a_{max}}{g} r_d = r_e \frac{\tau}{\sigma_{vo}'}$$

$$\underbrace{\begin{bmatrix} \sigma_v & 0 & 0 \\ 0 & \sigma_H & 0 \\ 0 & 0 & \sigma_H \end{bmatrix}}_{\sigma_o} + \underbrace{\begin{bmatrix} 0 & \tau & 0 \\ \tau & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}}_{\Delta\sigma} = \underbrace{\begin{bmatrix} \sigma_v & \tau & 0 \\ \tau & \sigma_H & 0 \\ 0 & 0 & \sigma_H \end{bmatrix}}_{\sigma}$$

Invariants

$$p_o' = \sigma_{vo}' \frac{1+2K_o}{3}$$

$$q_o = \sigma_{vo}' - \sigma_{ho}'$$

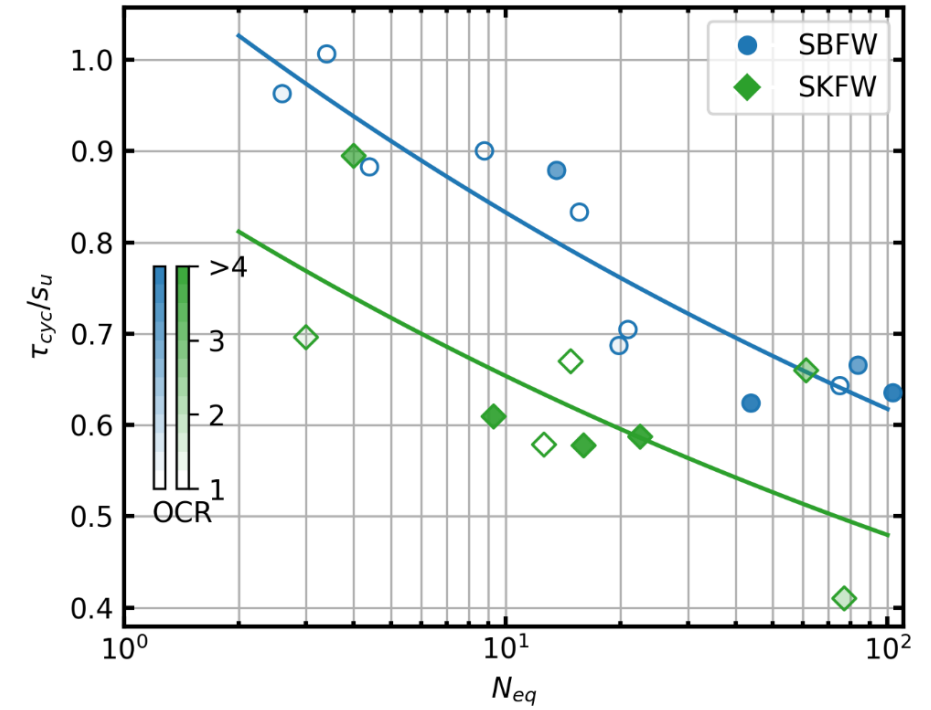
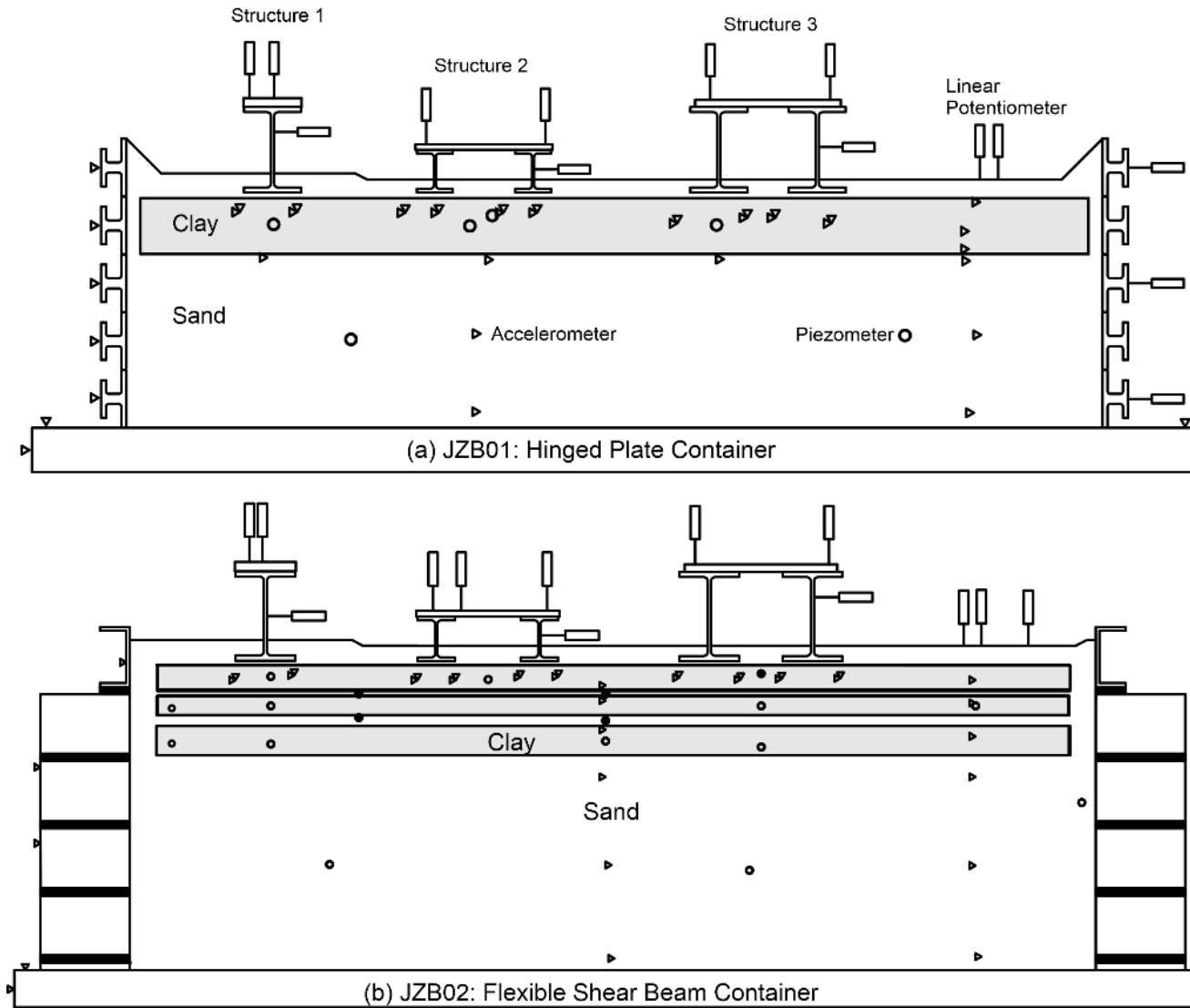
$$q = \sqrt{q_o'^2 + 3\tau^2}$$

$$CSR_q = r_e \frac{1+2K_o}{3p_o'} \sqrt{\frac{|q^2 - q_o'^2|}{3}} \text{sign}(q - q_o')$$

Invariant-based definition of cyclic stress ratio

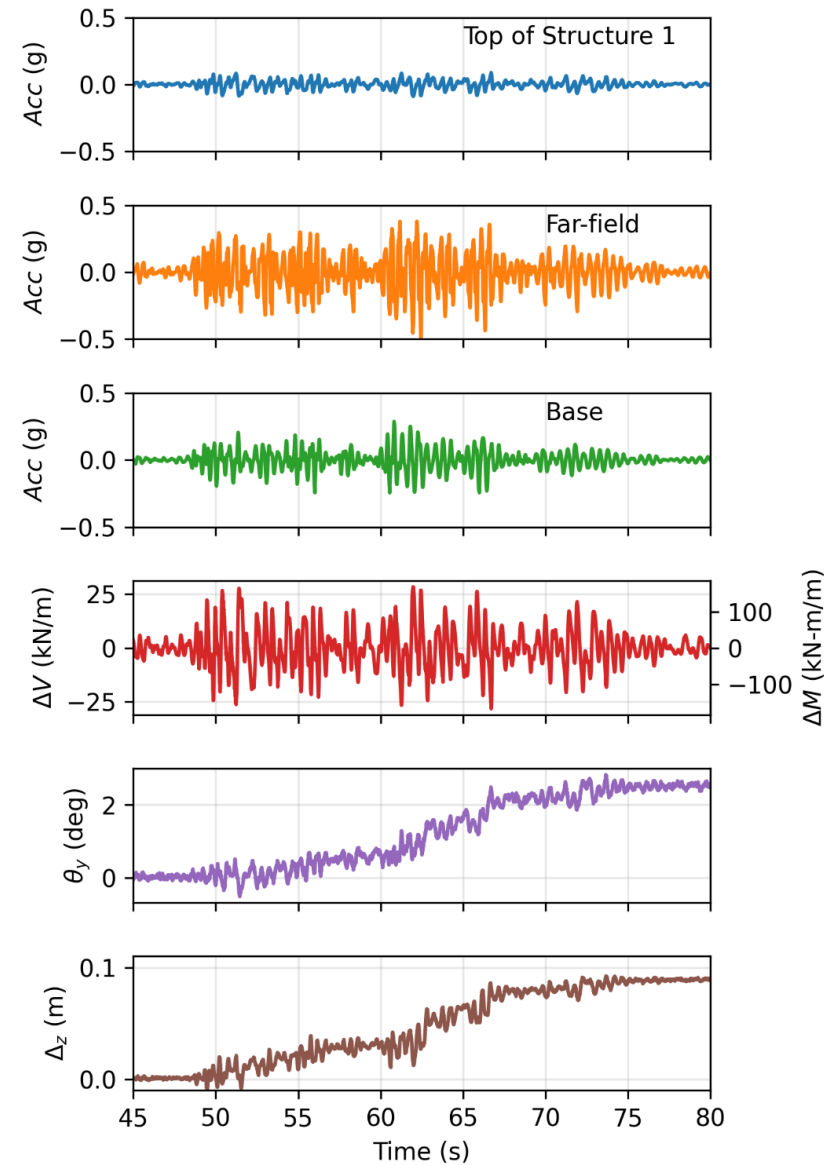
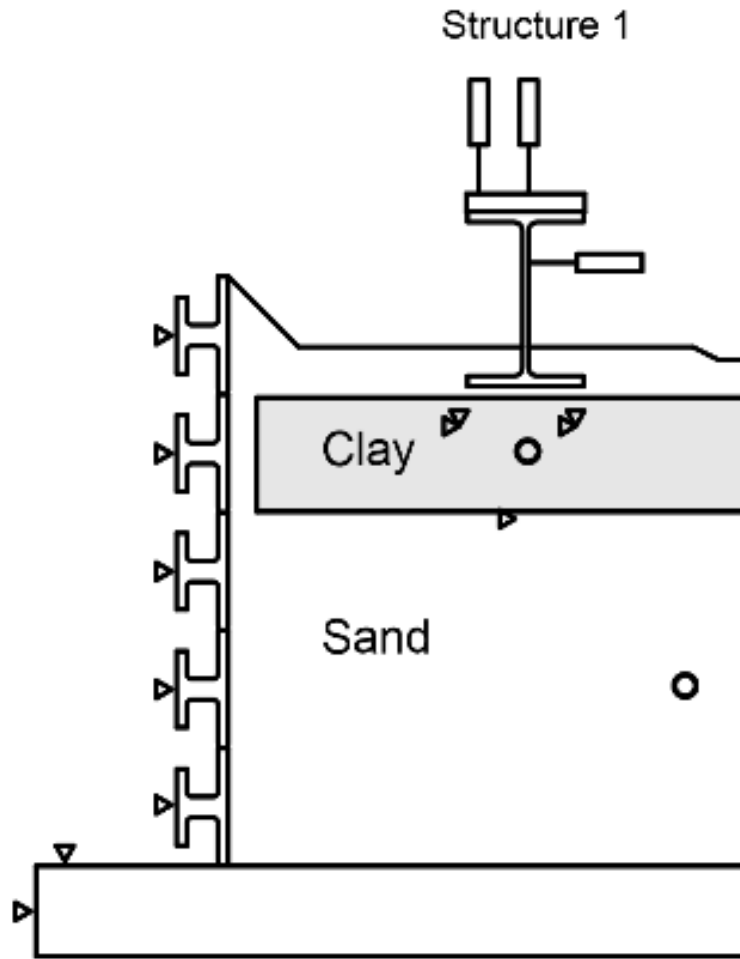
Brandenberg et al. (2022)

SSI Effects on Ground Failure



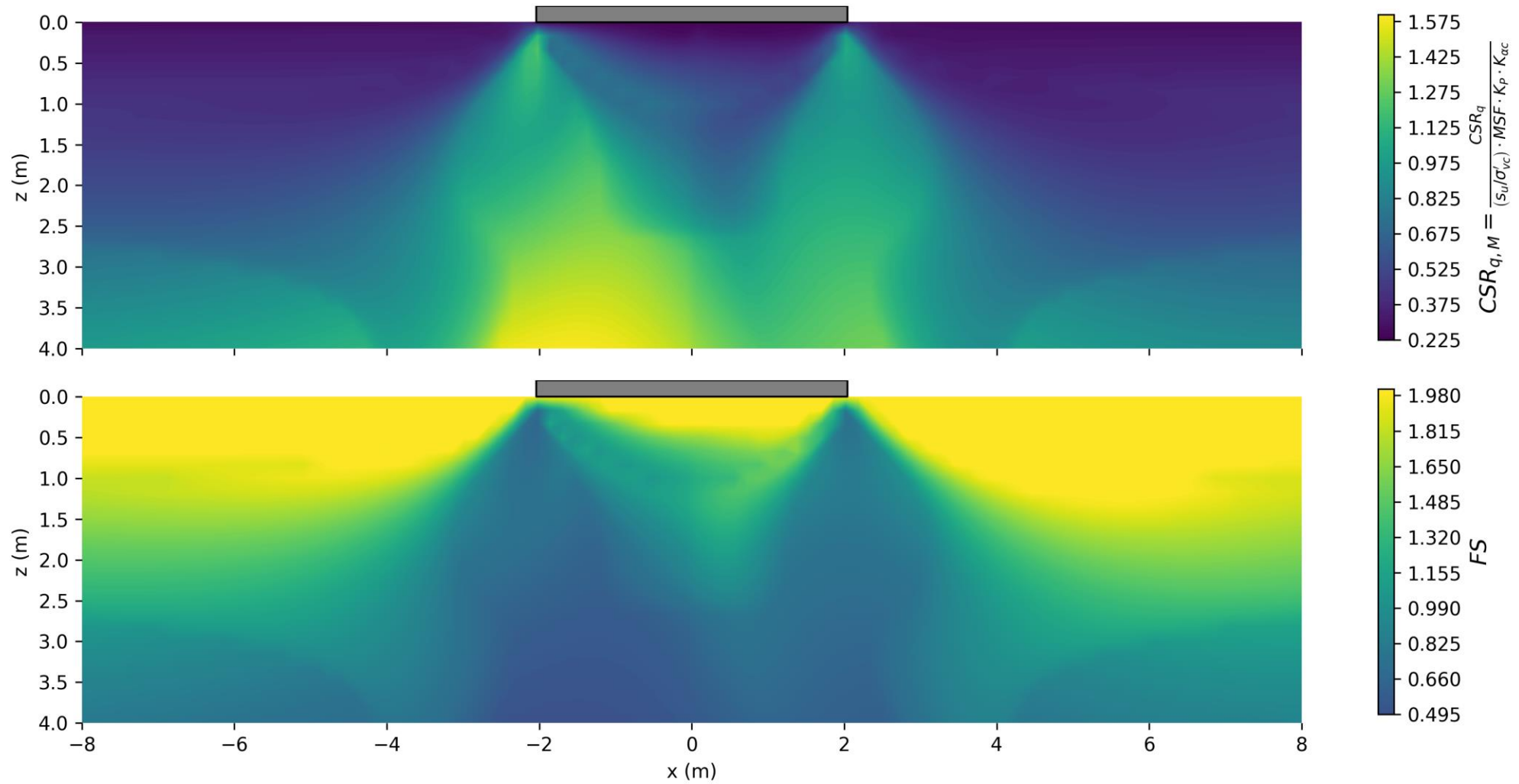
Brandenberg et al. (2022)

SSI Effects on Ground Failure



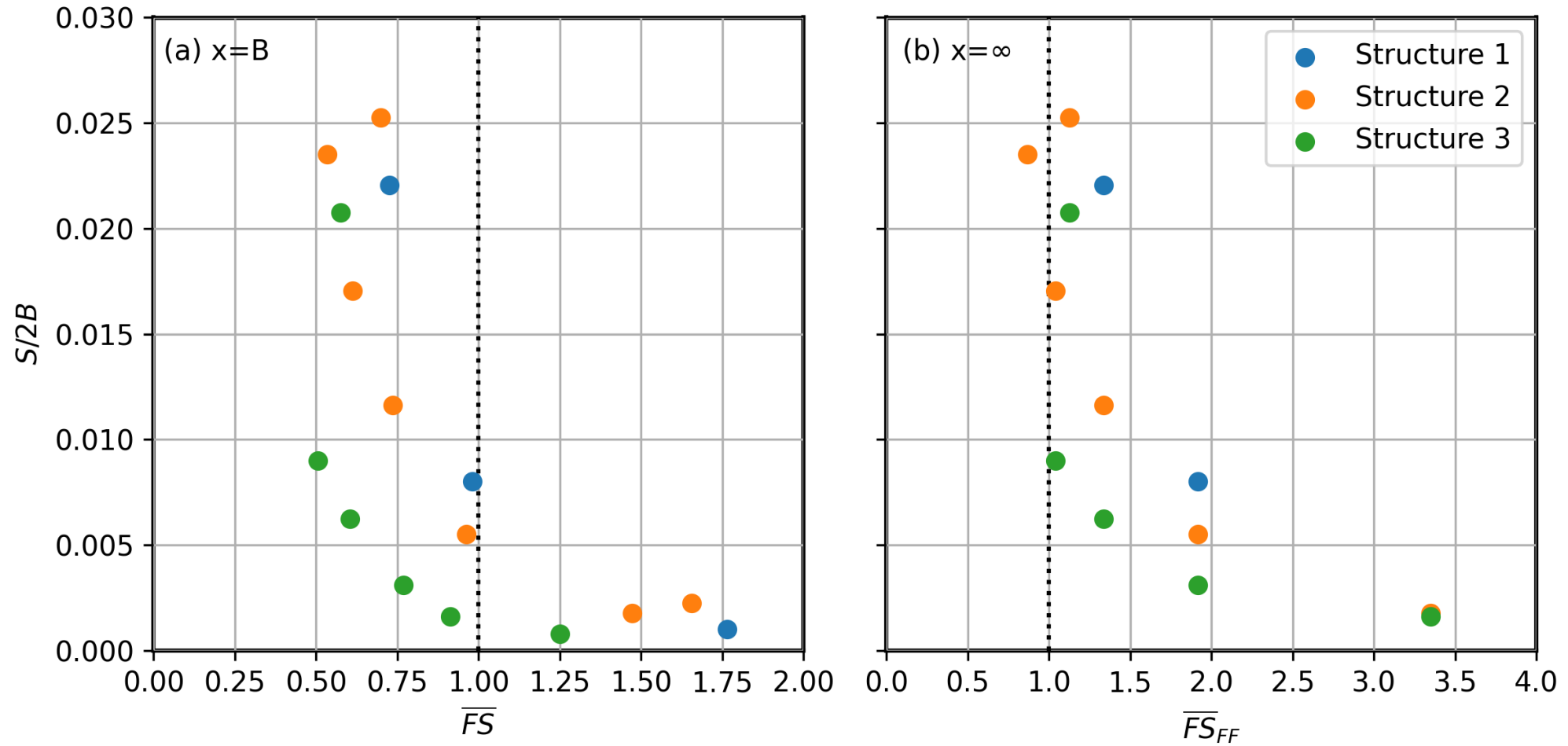
Brandenberg et al. (2022)

SSI Effects on Ground Failure



Brandenberg et al. (2022)

SSI Effects on Ground Failure



Brandenberg et al. (2022)

Conclusions

- Soil-structure interaction problems are inherently complex because they combine structural and geotechnical disciplines.
- Physical modeling studies provide key insights into fundamental mechanics that allow us to distill the problem into digestible units, and ultimately make design recommendations that are simple and straightforward to implement.
- Publishing experimental data is extremely important to facilitate these insights.

Conclusions

- I presented centrifuge modeling studies today.
- Structural models are necessarily simplified due to centrifuge scaling laws.
- There is tremendous need to validate SSI models using full-scale experiments, like those made possible by the UCSD shake table facility, because we are able to realistically model structural components

Acknowledgments

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